

方程式の計算（分数）

例題 次の方程式を解け。

(1) $2x - \frac{5}{4} = \frac{x}{3}$

答

(2) $\frac{1}{3}x - \frac{1}{2} = \frac{3}{4}x + \frac{2}{3}$

答

練習9A 次の方程式を解け。

(1) $\frac{x}{5} - \frac{x}{3} = 2$

答

(2) $8 - \frac{5}{6}x = -2$

答

(3) $\frac{2}{3}x + \frac{4}{5} = \frac{2}{3} - \frac{2}{5}x$

答

(4) $\frac{5}{6} - \frac{3}{4}x = \frac{2}{3} - \frac{1}{2}x$

答

練習B 次の方程式を解け。

(1) $\frac{1}{2}x - 2 = \frac{2}{3}$

答

(2) $\frac{3}{4}x - \frac{1}{2} = \frac{1}{4}x$

答

(3) $\frac{3}{4}x + 3 = 2x + \frac{1}{2}$

答

(4) $\frac{1}{2} + \frac{4}{3}x = \frac{2}{3} + \frac{3}{4}x$

答

(5) $-\frac{1}{2} + \frac{3}{4}x = \frac{1}{2}x - \frac{5}{8}$

答

(6) $-1 - \frac{5}{6}x = -x + \frac{1}{3}$

答

方程式の計算（分数）

例題 次の方程式を解け。

$$(1) 2x - \frac{5}{4} = \frac{x}{3}$$

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$$\begin{aligned} 2x \times 12 - \frac{5}{4} \times 12^3 &= \frac{x}{3} \times 12^4 \\ 24x - 15 &= 4x \\ 24x - 4x &= 15 \\ 20x &= 15 \\ \frac{1}{20} \times 20x &= \frac{3}{20} \times 15 \\ \frac{1}{20} \times 20x &= \frac{3}{4} \\ x &= \frac{3}{4} \end{aligned}$$

答 $x = \frac{3}{4}$

$$(2) \frac{1}{3}x - \frac{1}{2} = \frac{3}{4}x + \frac{2}{3}$$

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$$\begin{aligned} \frac{1}{3}x \times 12 - \frac{1}{2} \times 12^2 &= \frac{3}{4}x \times 12^3 + \frac{2}{3} \times 12^4 \\ 4x - 6 &= 9x + 8 \\ 4x - 9x &= 8 + 6 \\ -5x &= 14 \\ \frac{-1}{5} \times 5x &= \frac{14}{-5} \\ -1x &= -\frac{14}{5} \\ x &= -\frac{14}{5} \end{aligned}$$

答 $x = -\frac{14}{5}$

練習A 次の方程式を解け。

$$(1) \frac{x}{5} - \frac{x}{3} = 2$$

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$$\begin{aligned} \frac{x}{5} \times 15 - \frac{x}{3} \times 15 &= 2 \times 15 \\ 3x - 5x &= 30 \\ -2x &= 30 \\ \frac{-1}{2} \times 2x &= \frac{15}{-2} \times 30 \\ -1x &= -15 \\ x &= -15 \end{aligned}$$

答 $x = -15$

$$(2) 8 - \frac{5}{6}x = -2$$

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$$\begin{aligned} 8 \times 6 - \frac{5}{6}x \times 6 &= -2 \times 6 \\ 48 - 5x &= -12 \\ -5x &= -12 - 48 \\ \frac{-1}{5} \times 5x &= \frac{-12 - 48}{-5} \\ -1x &= -12 \\ x &= 12 \end{aligned}$$

答 $x = 12$

$$(3) \frac{2}{3}x + \frac{4}{5} = \frac{2}{3} - \frac{2}{5}x$$

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$$\begin{aligned} \frac{2}{3}x \times 15 + \frac{4}{5} \times 15^3 &= \frac{2}{3} \times 15^5 - \frac{2}{5}x \times 15^3 \\ 10x + 12 &= 10 - 6x \\ 10x + 6x &= 10 - 12 \\ 16x &= -2 \\ \frac{1}{16} \times 16x &= \frac{-1}{8} \\ \frac{1}{16} \times 16x &= -\frac{1}{8} \\ x &= -\frac{1}{8} \end{aligned}$$

答 $x = -\frac{1}{8}$

$$(4) \frac{5}{6} - \frac{3}{4}x = \frac{2}{3} - \frac{1}{2}x$$

★

$$\begin{aligned} \frac{5}{6} \times 12 - \frac{3}{4}x \times 12^3 &= \frac{2}{3} \times 12^4 - \frac{1}{2}x \times 12^6 \\ 10 - 9x &= 8 - 6x \\ -9x + 6x &= 8 - 10 \\ -3x &= -2 \\ \frac{-1}{3} \times 3x &= \frac{-2}{-3} \\ -1x &= -\frac{2}{3} \\ x &= \frac{2}{3} \end{aligned}$$

答 $x = \frac{2}{3}$

練習B 次の方程式を解け。

(1) $\frac{1}{2}x - 2 = \frac{2}{3}$

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$$\begin{aligned} \frac{1}{2}x \times 6 - 2 \times 6 &= \frac{2}{3} \times 6 \\ 3x - 12 &= 4 \\ 3x &= 4 + 12 \\ \frac{3x}{3} &= \frac{16}{3} \\ x &= \frac{16}{3} \end{aligned}$$

答

$$x = \frac{16}{3}$$

(2) $\frac{3}{4}x - \frac{1}{2} = \frac{1}{4}x$

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$$\begin{aligned} \frac{3}{4}x \times 4 - \frac{1}{2} \times 4 &= \frac{1}{4}x \times 4 \\ 9x - 2 &= x \\ 9x - x &= 2 \\ \frac{8x}{8} &= \frac{2}{8} \\ x &= \frac{1}{4} \end{aligned}$$

答

$$x = \frac{1}{4}$$

(3) $\frac{3}{4}x + 3 = 2x + \frac{1}{2}$

★

$$\begin{aligned} \frac{3}{4}x \times 4 + 3 \times 4 &= 2x \times 4 + \frac{1}{2} \times 4 \\ 3x + 12 &= 8x + 2 \\ 3x - 8x &= 2 - 12 \\ -5x &= -10 \\ \frac{-5x}{-5} &= \frac{-10}{-5} \\ x &= 2 \end{aligned}$$

答

$$x = 2$$

(4) $\frac{1}{2} + \frac{4}{3}x = \frac{2}{3} + \frac{3}{4}x$

★

$$\begin{aligned} \frac{1}{2} \times 12 + \frac{4}{3}x \times 12 &= \frac{2}{3} \times 12 + \frac{3}{4}x \times 12 \\ 6 + 16x &= 8 - 9x \\ 16x - 9x &= 8 - 6 \\ 7x &= 2 \\ \frac{7x}{7} &= \frac{2}{7} \\ x &= \frac{2}{7} \end{aligned}$$

答

$$x = \frac{2}{7}$$

(5) $-\frac{1}{2} + \frac{3}{4}x = \frac{1}{2}x - \frac{5}{8}$

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$$\begin{aligned} -\frac{1}{2} \times 8 + \frac{3}{4}x \times 8 &= \frac{1}{2}x \times 8 - \frac{5}{8} \times 8 \\ -4 + 6x &= 4x - 5 \\ 6x - 4x &= -5 + 4 \\ 2x &= -1 \\ \frac{2x}{2} &= \frac{-1}{2} \\ x &= -\frac{1}{2} \end{aligned}$$

答

$$x = -\frac{1}{2}$$

(6) $-1 - \frac{5}{6}x = -x + \frac{1}{3}$

★

$$\begin{aligned} -1 \times 6 - \frac{5}{6}x \times 6 &= -x \times 6 + \frac{1}{3} \times 6 \\ -6 - 5x &= -6x + 2 \\ -5x + 6x &= 2 + 6 \\ x &= 8 \end{aligned}$$

答

$$x = 8$$