

分配法則で展開して計算

例題 次の方程式を解け。

$$(1) \quad 2x - 5 = 3(4x - 5)$$

答

$$(2) \quad 4x - 4(3x + 2) = 8$$

答

$$(3) \quad x - 3 - (7x - 1) = 8 + 2x$$

答

練習A 次の方程式を解け。

$$(1) \quad x + 6 = -3(2x + 5)$$

答

$$(3) \quad 16 - (5x - 8) = 19$$

答

$$(5) \quad 3x - 2(x - 5) = -12$$

答

$$(2) \quad 2(3 - 4x) = 2x + 8$$

答

$$(4) \quad -13 = 6 - 2(3x - 1)$$

答

$$(6) \quad 15 - 2(x - 4) = 3x + 8$$

答

練習B 次の方程式を解け。

(1) $3x - 6 = 2(6 - 3x)$

答

(4) $x - 8 - (3x + 1) = -7$

答

(7) $2x + 4 - (x + 7) = 12 - 4x$

答

(2) $-11 + 5x = 2(4x - 3)$

答

(5) $13 = 9 - 4(x + 8)$

答

(8) $4 - 2(3 - 2x) = 6x - 4$

答

(3) $-3(x + 6) = 4(x - 3)$

答

(6) $7x - 4(3x + 5) = -40$

答

(9) $8(3 + x) = 10 - 5(x + 5)$

答

分配法則で展開して計算

例題 次の方程式を解け。

(1) $2x-5=3(4x-5)$

$$\begin{aligned} \star & 2x-5=3\times 4x+3\times(-5) \\ & 2x-5=12x-15 \\ & 2x-12x=-15+5 \\ & -10x=-10 \\ & \frac{-10x}{-10_1}=\frac{-10}{-10_1} \\ & x=1 \end{aligned}$$

答 $x=1$

(2) $4x-4(3x+2)=8$

$$\begin{aligned} \star & 4x-4\times 3x-4\times 2=8 \\ & 4x-12x-8=8 \\ & 4x-12x=8+8 \\ & -8x=16 \\ & \frac{-8x}{-8_1}=\frac{16}{-8_1} \\ & x=-2 \end{aligned}$$

答 $x=-2$

(3) $x-3-(7x-1)=8+2x$

$$\begin{aligned} \star & x-3-7x+1=8+2x \\ & x-7x-2x=8+3-1 \\ & -8x=10 \\ & \frac{-8x}{-8_1}=\frac{10}{-8_4} \\ & x=-\frac{5}{4} \end{aligned}$$

答 $x=-\frac{5}{4}$

練習A 次の方程式を解け。

(1) $x+6=-3(2x+5)$

$$\begin{aligned} \star & x+6=-3\times 2x-3\times 5 \\ & x+6=-6x-15 \\ & x+6x=-15-6 \\ & 7x=-21 \\ & \frac{7x}{7_1}=\frac{-21}{7_1} \\ & x=-3 \end{aligned}$$

答 $x=-3$

(3) $16-(5x-8)=19$

$$\begin{aligned} \star & 16-5x+8=19 \\ & -5x=19-16-8 \\ & -5x=-5 \\ & \frac{-5x}{-5_1}=\frac{-5}{-5_1} \\ & x=1 \end{aligned}$$

答 $x=1$

(5) $3x-2(x-5)=-12$

$$\begin{aligned} \star & 3x-2\times x-2\times(-5)=-12 \\ & 3x-2x+10=-12 \\ & 3x-2x=-12-10 \\ & x=-22 \end{aligned}$$

答 $x=-22$

(2) $2(3-4x)=2x+8$

$$\begin{aligned} \star & 2\times 3+2\times(-4x)=2x+8 \\ & 6-8x=2x+8 \\ & -8x-2x=8-6 \\ & -10x=2 \\ & \frac{-10x}{-10_1}=\frac{2}{-10_5} \\ & x=-\frac{1}{5} \end{aligned}$$

答 $x=-\frac{1}{5}$

(4) $-13=6-2(3x-1)$

$$\begin{aligned} \star & -13=6-2\times 3x-2\times(-1) \\ & -13=6-6x+2 \\ & 6x=6+2+13 \\ & 6x=21 \\ & \frac{6x}{6_1}=\frac{21}{6_2} \\ & x=\frac{7}{2} \end{aligned}$$

答 $x=\frac{7}{2}$

(6) $15-2(x-4)=3x+8$

$$\begin{aligned} \star & 15-2\times x-2\times(-4)=3x+8 \\ & 15-2x+8=3x+8 \\ & -2x-3x=8-15-8 \\ & -5x=-15 \\ & \frac{-5x}{-5_1}=\frac{-15}{-5_1} \\ & x=3 \end{aligned}$$

答 $x=3$

練習B 次の方程式を解け。

(1) $3x - 6 = 2(6 - 3x)$

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$$\begin{aligned} 3x - 6 &= 2 \times 6 + 2 \times (-3x) \\ 3x - 6 &= 12 - 6x \\ 3x + 6x &= 12 + 6 \\ 9x &= 18 \\ \frac{1}{9} \cancel{x} &= \frac{2}{9} \cancel{18} \\ x &= 2 \end{aligned}$$

答 $x = 2$

(2) $-11 + 5x = 2(4x - 3)$

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$$\begin{aligned} -11 + 5x &= 2 \times 4x + 2 \times (-3) \\ -11 + 5x &= 8x - 6 \\ 5x - 8x &= -6 + 11 \\ -3x &= 5 \\ \frac{-1}{3} \cancel{x} &= \frac{5}{-3} \\ x &= -\frac{5}{3} \end{aligned}$$

答 $x = -\frac{5}{3}$

(3) $-3(x+6) = 4(x-3)$

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$$\begin{aligned} -3x - 3 \times 6 &= 4x + 4 \times (-3) \\ -3x - 18 &= 4x - 12 \\ -3x - 4x &= -12 + 18 \\ -7x &= 6 \\ \frac{-1}{7} \cancel{x} &= \frac{6}{-7} \\ x &= -\frac{6}{7} \end{aligned}$$

答 $x = -\frac{6}{7}$

(4) $x - 8 - (3x + 1) = -7$

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$$\begin{aligned} x - 8 - 3x - 1 &= -7 \\ x - 3x &= -7 + 8 + 1 \\ -2x &= 2 \\ \frac{-1}{2} \cancel{x} &= \frac{1}{-2} \cancel{2} \\ x &= -1 \end{aligned}$$

答 $x = -1$

(5) $13 = 9 - 4(x+8)$

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$$\begin{aligned} 13 &= 9 - 4 \times x - 4 \times 8 \\ 13 &= 9 - 4x - 32 \\ 4x &= 9 - 32 - 13 \\ 4x &= -36 \\ \frac{1}{4} \cancel{x} &= \frac{-9}{4} \cancel{36} \\ x &= -9 \end{aligned}$$

答 $x = -9$

(6) $7x - 4(3x+5) = -40$

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$$\begin{aligned} 7x - 4 \times 3x - 4 \times 5 &= -40 \\ 7x - 12x - 20 &= -40 \\ 7x - 12x &= -40 + 20 \\ -5x &= -20 \\ \frac{-1}{5} \cancel{x} &= \frac{-4}{-5} \cancel{20} \\ x &= 4 \end{aligned}$$

答 $x = 4$

(7) $2x + 4 - (x+7) = 12 - 4x$

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$$\begin{aligned} 2x + 4 - x - 7 &= 12 - 4x \\ 2x - x + 4x &= 12 - 4 + 7 \\ 5x &= 15 \\ \frac{1}{5} \cancel{x} &= \frac{3}{5} \cancel{15} \\ x &= 3 \end{aligned}$$

答 $x = 3$

(8) $4 - 2(3 - 2x) = 6x - 4$

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$$\begin{aligned} 4 - 2 \times 3 - 2 \times (-2x) &= 6x - 4 \\ 4 - 6 + 4x &= 6x - 4 \\ 4x - 6x &= -4 - 4 + 6 \\ -2x &= -2 \\ \frac{-1}{2} \cancel{x} &= \frac{-1}{-2} \cancel{2} \\ x &= 1 \end{aligned}$$

答 $x = 1$

(9) $8(3+x) = 10 - 5(x+5)$

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$$\begin{aligned} 8 \times 3 + 8 \times x &= 10 - 5 \times x - 5 \times 5 \\ 24 + 8x &= 10 - 5x - 25 \\ 8x + 5x &= 10 - 25 - 24 \\ 13x &= -39 \\ \frac{1}{13} \cancel{x} &= \frac{-3}{13} \cancel{39} \\ x &= -3 \end{aligned}$$

答 $x = -3$